

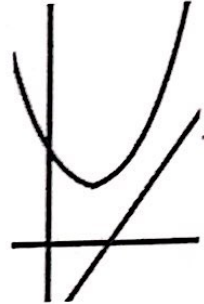
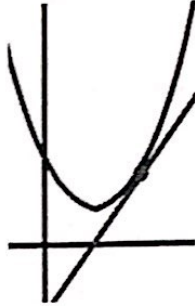
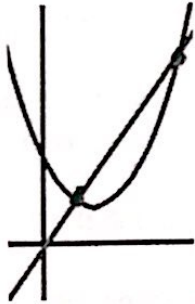
# HW = Day 16

Name: \_\_\_\_\_

Date: \_\_\_\_\_

As you know, systems have 2 or more equations. A Linear-Quadratic System of Equations involves a line and a parabola.

The solution is the point(s) where the line intersects with the parabola. There can be one, two, or no solutions to this type of system.



2 solutions

1 solution

None solutions

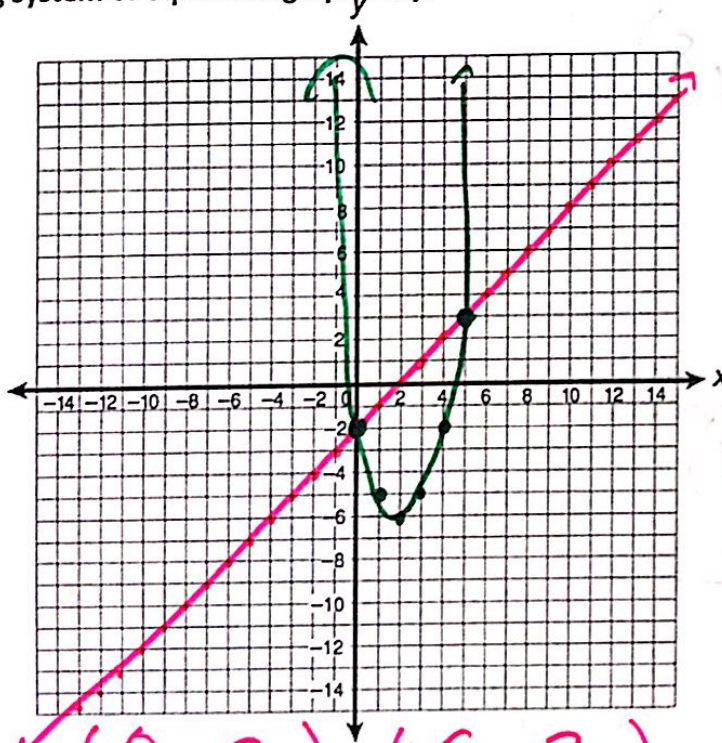
## Example 1: Solving Linear-Quadratic Systems by Graphing.

Solve the following system of equations graphically:

$$y = x^2 - 4x - 2$$

$$y = x - 2$$

x	y
0	-2
1	-5
2	-6
3	-5
4	-2



$$x^2 - 4x + 4 = 2 + 4$$

$$(x - 2)^2 = 6$$

$$(x - 2)^2 - 6 = y$$

**Step 1:** Make sure all the equations are either in  $y = mx + b$  or  $y = ax^2 + bx + c$  form.

**Step 2:** Graph the line

**Step 3:** Graph the parabola, using the line of symmetry ( $x = -b/2a$  as a starting point)

**Step 4:** Find the intersection points

$$25 - 20 - 2 = 3 - 2 = 3$$

$$1 - 4 - 2 = -5$$

$$1 - 6 = -5$$

$$5, 3$$

Solution(s): (0, -2) (5, 3)

Check:

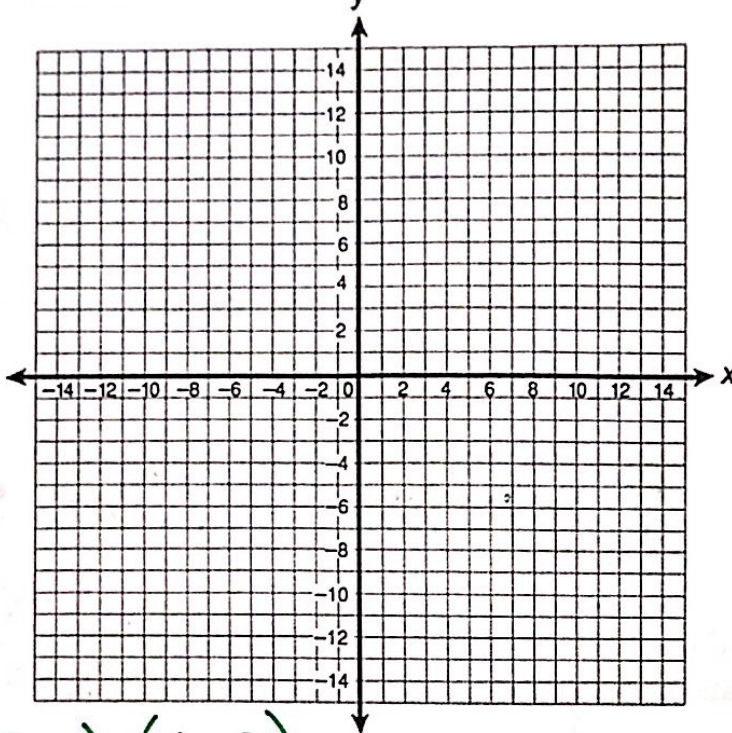
$y = 0^2 - 4(0) - 2 = -2$ $y = 0 - 2 = -2$	$y = 5^2 - 4(5) - 2 = 25 - 20 - 2 = 3$ $y = 5 - 2 = 3$
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**You Try 1!**

Solve the following system of equations graphically:

$y = x^2 + 4x + 3$   
 $y = 2x + 6$

x	y



**Step 1:** Make sure all the equations are either in  $y = mx + b$  or  $y = ax^2 + bx + c$  form.

**Step 2:** Graph the line

**Step 3:** Graph the parabola, using the line of symmetry ( $x = -b/2a$  as a starting point)

**Step 4:** Find the intersection points

Solution(s):  $(-3, 0) (1, 8)$

Check:

**Example 2A: Solving Linear-Quadratic Systems Algebraically**

Solve the system of equations algebraically.

$y = x^2 - x - 6$   
 $y = 2x - 2$

substitution

$2x - 2 = x^2 - x - 6$   
 $-2x + 2 \quad -2x + 12$

$0 = x^2 - 3x - 4$

$(x + 1)(x - 4)$

$x = -1, 4$

$(-1, -4)$   
 $(4, 6)$

Check!

In calc.  
 put  $x^2 - x - 6$  in  $Y_1$   
 put  $2x - 2$  in  $Y_2$   
 2nd trace intersect.

Name: \_\_\_\_\_

Date: \_\_\_\_\_

### Example 2B: Solving Linear-Quadratic Systems Algebraically

Solve the system of equations algebraically.

$$y = x^2 - x - 6$$

$$y = x - 10$$

Check!

$$\begin{aligned} x-10 &= x^2 - x - 6 \\ 0 &= x^2 - 2x + 4 \\ x^2 - 2x + 1 &= -4 + 1 \\ (x-1)^2 &= -3 \end{aligned}$$

No Solution!

You Try 2!

$$x = 1 \pm i\sqrt{3}$$

$$\begin{aligned} x^2 + y &= -14 \\ x - y &= 6 \end{aligned}$$

Check:

$$\begin{aligned} y &= x^2 \\ y &= 2x + 3 \end{aligned}$$

Check: